

# Hypothesis Test Statistics and Confidence Intervals

<u>1 - <math>\alpha</math> Confidence Interval</u> Point Estimate $\pm$ Maximum Error $E$	<u>Hypothesis Test Value (Statistic)</u> NULL Hypothesis: Use the statement containing the condition of equality ( $=$ or $\geq$ ), either directly or implied, as the Null Hypothesis $H_0$ .
(TI-83, TI-86)	(TI-83, TI-86)
<b>Single Population</b>	
<b>One Sample for mean <math>\mu</math> (<math>\sigma</math> is known)</b>	
(ZInterval, ZInt1)	(Z-Test, ZTest)
$\bar{x} \pm Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$	Use the Normal $Z$ -Table for the critical value $Z$ $Z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$
<b>One Sample for mean <math>\mu</math> (<math>\sigma</math> is unknown)</b>	
(TInterval, TInt1)	(T-Test, TTest)
$\bar{x} \pm t_{\alpha/2} \frac{s}{\sqrt{n}}$	$df = n - 1$ Use the $t$ -distribution Table for the critical value $t$ $t = \frac{\bar{x} - \mu}{s/\sqrt{n}}$
<b>One Sample for Proportion <math>p</math></b>	
(1-PropZInt, ZPin1)	(1-PropZTest, ZPrp1)
$\hat{p} \pm Z_{\alpha/2} \sqrt{\frac{\hat{p}\hat{q}}{n}}$	Use the Normal $Z$ -Table for the critical value $Z$ $Z = \frac{\hat{p} - p}{\sqrt{pq/n}}$
(TI-83, TI-86)	(TI-83, TI-86)
<b>Dual Populations</b>	
<b>Dependent Paired for <math>\mu_d</math></b>	
(TInterval, TInt1)	(T-Test, TTest)
$\bar{d} \pm t_{\alpha/2} \frac{s_d}{\sqrt{n}}$	$df = n - 1$ Use the $t$ -distribution Table for the critical value $t$ $t = \frac{\bar{d} - \mu_d}{s_d/\sqrt{n}}$ Use $\mu_d = 0$
<b>Two Independent Samples for <math>\mu_1 - \mu_2</math> (<math>\sigma_1, \sigma_2</math> are known)</b>	
(2-SampZInt, ZInt2)	(2-SampZTest, Zsam2)
$(\bar{x}_1 - \bar{x}_2) \pm Z_{\alpha/2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$	Use the Normal $Z$ -Table for the critical value $Z$ $Z = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$ Use $\mu_1 - \mu_2 = 0$
<b>Two Independent Samples for <math>\mu_1 - \mu_2</math> (<math>\sigma_1, \sigma_2</math> are unknown)</b>	
(2-SampTInt, TInt2)	(2-SampTTest, Tsam2)
$(\bar{x}_1 - \bar{x}_2) \pm t_{\alpha/2} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$	$df = \text{smaller of } n_1 - 1 \text{ or } n_2 - 1$ Use the $t$ -distribution Table for the critical value $t$ Use "NOT POOLED" on the calculator. $t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$ Use $\mu_1 - \mu_2 = 0$
<b>Two Independent Samples for Proportions <math>p_1 - p_2</math></b>	
(2-PropZInt, ZPin2)	(2-PropZTest, ZPrp2)
$(\hat{p}_1 - \hat{p}_2) \pm Z_{\alpha/2} \sqrt{\frac{\hat{p}_1\hat{q}_1}{n_1} + \frac{\hat{p}_2\hat{q}_2}{n_2}}$	Use the Normal $Z$ -Table for the critical value $Z$ $n\bar{p} \geq 5$ and $n\bar{q} \geq 5$ for both samples $Z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\sqrt{\frac{\hat{p}\hat{q}}{n_1} + \frac{\hat{p}\hat{q}}{n_2}}}$ Use $p_1 - p_2 = 0$
where, $\bar{p} = \frac{x_1 + x_2}{n_1 + n_2}$ or $\bar{p} = \frac{n_1\hat{p}_1 + n_2\hat{p}_2}{n_1 + n_2}$ $\bar{q} = 1 - \bar{p}$	
<b>1-Prop:</b> $p = \frac{X}{N}$ $\hat{p} = \frac{x}{n}$ $q = 1 - p$ $\hat{q} = 1 - \hat{p}$ <b>Dual Prop:</b> $p_1 = \frac{X_1}{N_1}$ $p_2 = \frac{X_2}{N_2}$ $\hat{p}_1 = \frac{x_1}{n_1}$ $\hat{p}_2 = \frac{x_2}{n_2}$ $\bar{p} = \frac{x_1 + x_2}{n_1 + n_2}$ or $\bar{p} = \frac{n_1\hat{p}_1 + n_2\hat{p}_2}{n_1 + n_2}$ $q_1 = 1 - p_1$ $q_2 = 1 - p_2$ $\hat{q}_1 = 1 - \hat{p}_1$ $\hat{q}_2 = 1 - \hat{p}_2$ $\bar{q} = 1 - \bar{p}$	
<b>Sample Size Determination</b>	
for Mean $\mu$ $n = \frac{Z_{\alpha/2}^2 \sigma^2}{E^2} = \left( \frac{Z_{\alpha/2} \sigma}{E} \right)^2$	for the Proportion $p$ $n = \frac{Z_{\alpha/2}^2 pq}{E^2}$ or use $n = \frac{Z_{\alpha/2}^2 (.25)}{E^2}$ (round up)    (if $p, q$ unknown)